

Collective action

GT

- ① Nonexcludable: A person who has not contributed & incurred a cost cannot be prevented from enjoying the benefits.
- ② Nonrival: No person's benefits are diminished by the fact that someone else is also enjoying the benefits.

A project with properties ① & ② is a pure public good project.

e.g. Public infrastructure.

e.g. 2 Farmer Irrigation Project.

Cost = $C(n)$ ← # of people involved

e.g. $C(1) = 7$ $C(2) = 4$
 ↑
 Cost per farmer
 $B(1) = 6$ $B(2) = 8$

Benefits = $B(n)$

$$P(n) = \text{Payoff} = B(n) - C(n)$$

		II	
		Build	Not
I	Build	4, 4	-1, 6
	Not	6, -1	0, 0

Not building is the dominant strategy. Same as Hawk Strategy in PD.
 Social optimum is (build, build) outcome.

free rider: it is best to reap benefits of other players
 alternative example: $C(1) = 4$, $C(2) = 3$ then

		II	
		B	Not
I	B	5, 5	2, 6
	Not	6, 2	0, 0

$$\text{Social optima} = 10 > 2 + 6$$

Large groups

Consider N farmers $C(n) = \text{Cost}$ $B(n) = \text{Benefit}$

$$P(n) = B(n) - C(n) = \text{Payoff for a Participant}$$

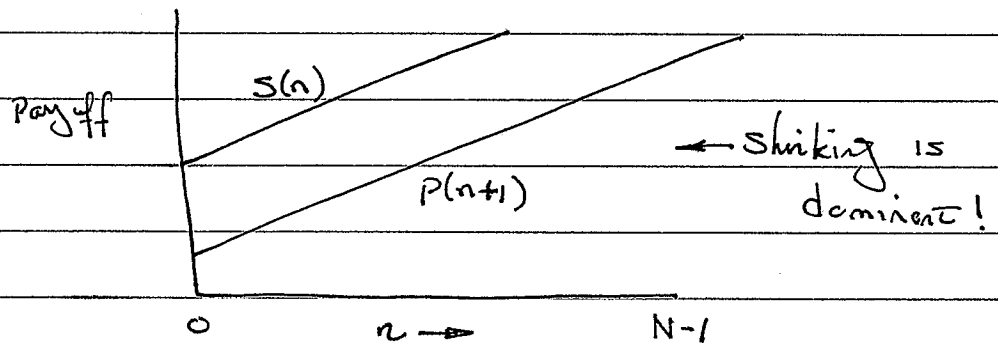
$$S(n) = B(n) = \text{shirker Benefit}$$

Consider $N-1$ others ...

- n Participants
- $(N-1-n)$ Shirkers

If $P(n+1) > S(n) \rightarrow$ Participate

If $P(n+1) < S(n) \rightarrow$ Shirk



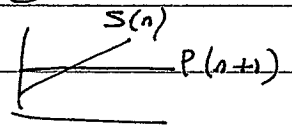
$$T(n) = \text{Social Payoff} = n \cdot P(n) + (N-n) S(n)$$

$$= N S(n) - n [S(n) - P(n)]$$

We seek value of n to maximize $T(n)$ for social optimum.

Society benefits most iff all participated.

Nash Equil iff $S(n)$ & $P(n+1)$ intersect.



Externality

E.g. 8000 Commuters driving from city & suburb
Expressway (P), Local Roads (S)

15 min uncongested \uparrow 45 min regardless of volume

\downarrow If driver increases volume for all drivers by 0.005 min ($\approx \frac{1}{4}$ second)

Payoff = minutes of time saved from one hour.

For local roads: $S(n) = 60 - 45 = 15$ min invariant on n .

For Expressway: $P(n) = \begin{cases} 60 - 15 = 45 & \text{for } n = 0 \\ 45 - 0.005n & \text{depends on } n. \end{cases}$

E.g. if 4000 cars on expressway, $n = 4000$; $15 \times 4000 \times 0.005 = 35$ min
Commuter Time

$$P(4000) = 60 - 35 = 25 \text{ min}$$

If one person (you) switch from local to expressway, $\exists 4001$ cars

$$\text{Commuter Time} = 4001 \times 0.005 = 35.005 \text{ min}$$

$$P(n+1) = P(4001) = 24.995 \text{ min}$$

$$\left. \begin{matrix} P(n+1) > S(n) \\ 24.995 > 15 \end{matrix} \right\} \Rightarrow \text{Private Incentive to Switch}$$

marginal Private gain $= P(n+1) - S(n) = 9.995$ min

Effect For others: $P(4001) - P(4000) = -0.005$ For expressway drivers $\rightarrow -20$ min

$$P(4001) - S(4000) = 0 \text{ For local drivers.}$$

Externality (Spillover effect) \equiv when one person's action affects others.

Marginal Social gain \equiv marginal Private gain + marginal Spillover effect on society. gain might be positive or negative

$$\text{marginal Social gain} = (4000 \times -0.005) + 9.995 = -10.005$$

negative impact

General Case

GT

let $T(n) =$ Social Payoff function

↳ # of people choosing P. So $N-n$ choose S
let n people choose P, one person switches from S to P,

$$T(n+1) = (n+1) \cdot P(n+1) + [N - (n+1)] S(n+1)$$

$$T(n+1) - T(n) = \underbrace{(P(n+1) - S(n))}_{\text{marginal private gain of switcher}} + \underbrace{n [P(n+1) - P(n)]}_{\text{loss of local driver}} + \underbrace{[N - (n+1)] [S(n+1) - S(n)]}_{\text{marginal spillover effect on others}}$$

marginal private gain
of switcher

loss of
local driver

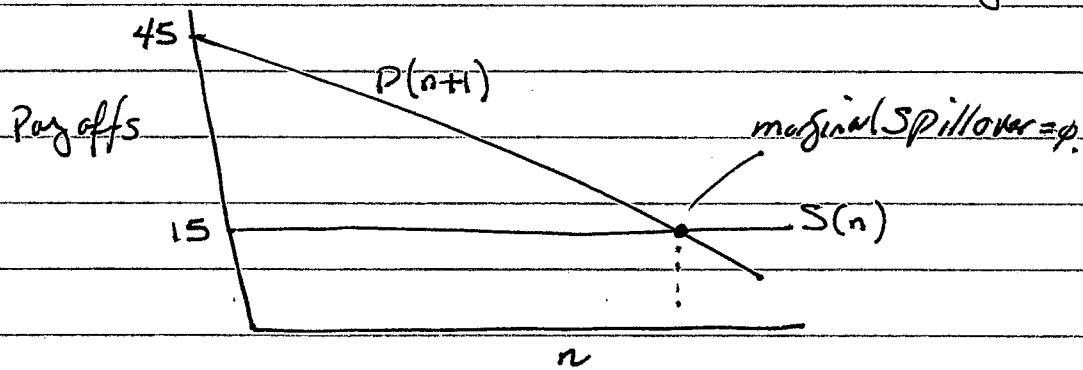
marginal spillover
effect on
others

if n is very large we will not look at one person difference but
a rate of change $T'(n) dn$

$$\text{Since } T(n) = n \cdot P(n) + (N-n) S(n).$$

$$T'(n) = P(n) + n P'(n) - S'(n) + (N-n) S'(n)$$

$$= \underbrace{[P(n) - S(n)]}_{\text{marginal social gain}} + \underbrace{n P'(n) + (N-n) S'(n)}_{\text{marginal private gain}}$$



Internalizing externalities: making each person pay for social externalities,
e.g., taxes, tolls